

$$F_{t+1}(n) = (F_t(n) + (-1)^t f_t + (1)^t f_{t+N}) e^{2\pi i \frac{n}{N}}$$